

Cooperation in Cognitive Radio Networks

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Source: W. Saad and H. V. Poor, “Cooperation in Cognitive Radio Networks: From Monitoring to Access.” In *Mechanisms and Games for Dynamic Spectrum Allocation*, T. Alpcan, et al., Eds. (Cambridge University Press, 2014)

Supported in part by the National Science Foundation under Grant ECCS-1343210.



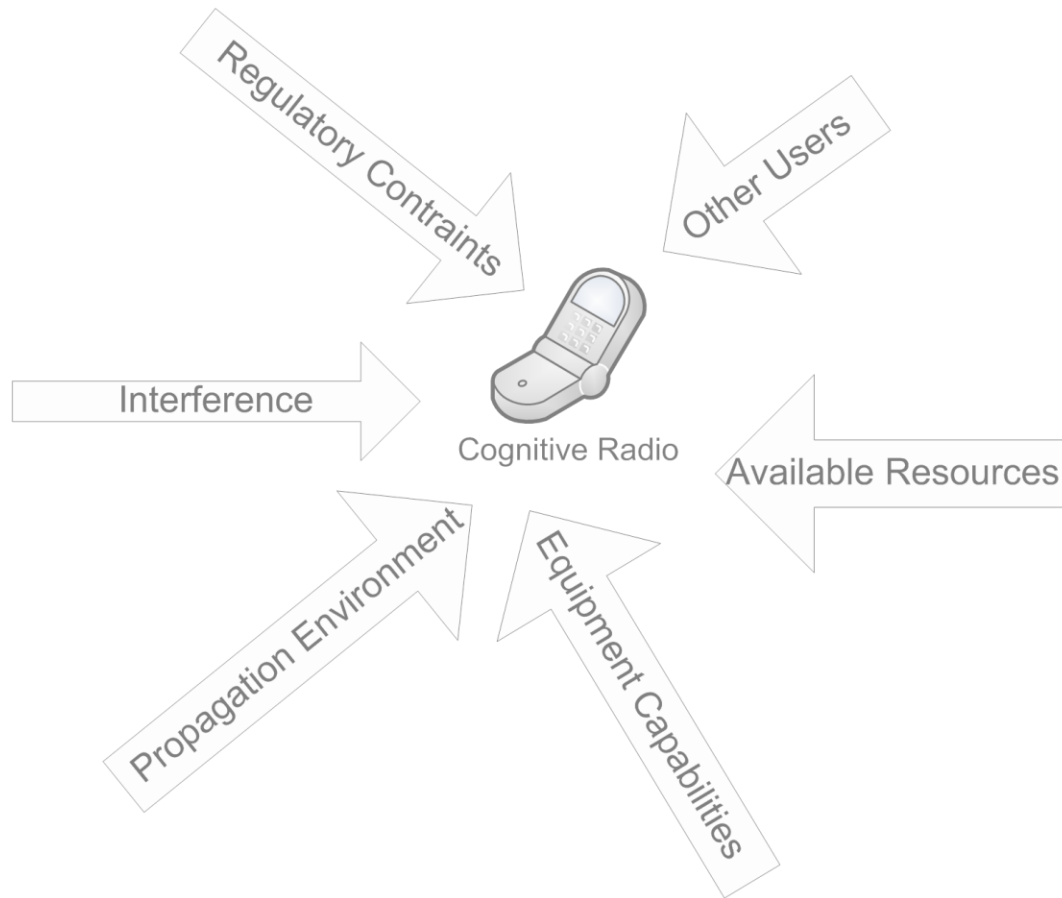
Outline

1. Background and Motivation
2. Spectrum Sensing and Sharing
3. Spectrum Monitoring
4. Summary

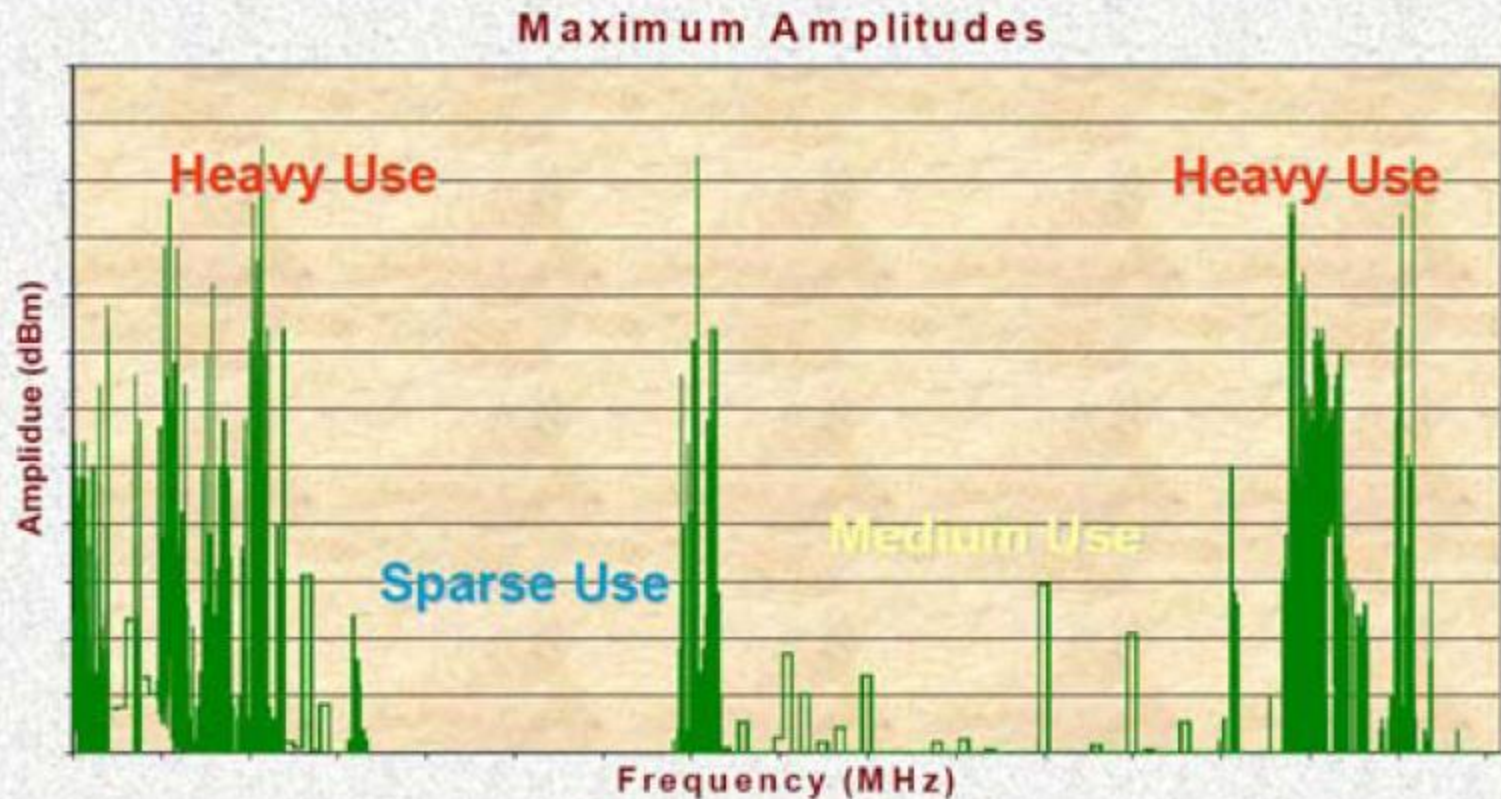
Background
And
Motivation

Cognitive Radio

A **cognitive radio** is a radio that is able to **sense, adapt** and **learn** from its operating environment.

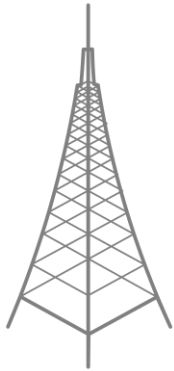


Spectrum Occupancy



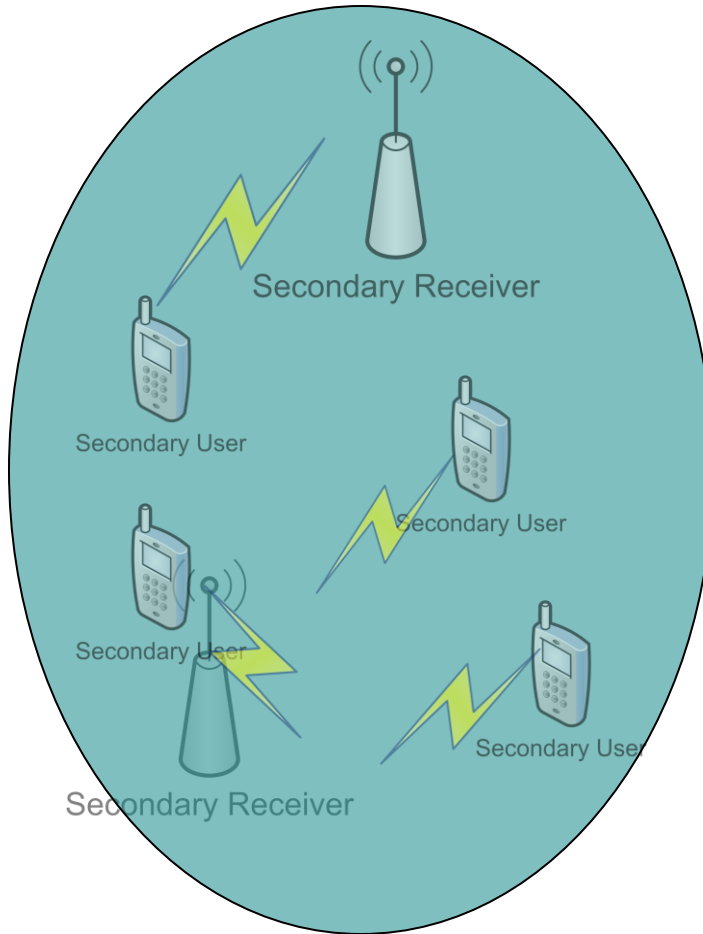
Source: FCC, Spectrum Policy Task Force, Technology Advisory Council (TAC) Briefing (December 2002).

Cognitive Radio In a Nutshell

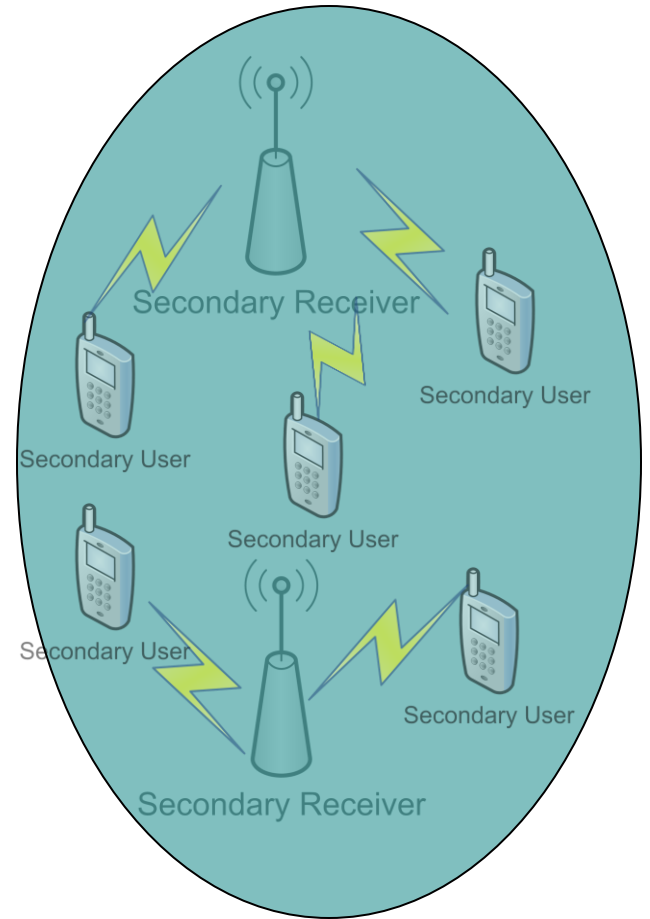


Primary User
(Licensed user)

e.g. TV
Transmitter



Secondary Network 1



Secondary Network 2

Cognitive Radio: Challenges

- **Spectrum sharing**
 - How to share the spectrum among the users?
 - Scheduling and resource allocation (e.g. channel allocation)
- **Spectrum sensing**
 - How to detect unused spectrum?
 - The spectrum sensing problem is basically a decision between two hypotheses: the primary user is absent/present
- **Spectrum monitoring**
 - How to generate models for the activity of the primary user?
 - Monitoring and evaluating the transmission patterns of primary users; machine learning

Spectrum Sensing and Sharing

Motivation and Model

- How can secondary users jointly sense and share the spectrum in a multi-channel cognitive network?
 - Sense to detect the best channel vs. time used for sensing
 - Accessing a vacant channel vs. waiting to find a better channel
 - Exploration vs. exploitation tradeoff
- Consider a multi-channel network with K PUs (channels) that are being sensed/accessed by N SUs:
 - Each PU channel is available with probability ϑ_k
 - An SU can only sense a subset of the K channels

Formalism

- Each SU aims at **optimizing** the following **utility**:

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Capacity achieved by SU i over channel k_j under “average” interference from other SUs

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$$\tau_i(\mathcal{K}_i^{\text{ord}}) = \sum_{j=1}^{K_i} \left(j \cdot \alpha \cdot \theta_{k_j} \prod_{m=1}^{j-1} (1 - \theta_{k_m}) \right) + \prod_{l=1}^{K_i} (1 - \theta_{k_l})$$

Average sensing time with α being the fraction of time needed to sense **one channel**

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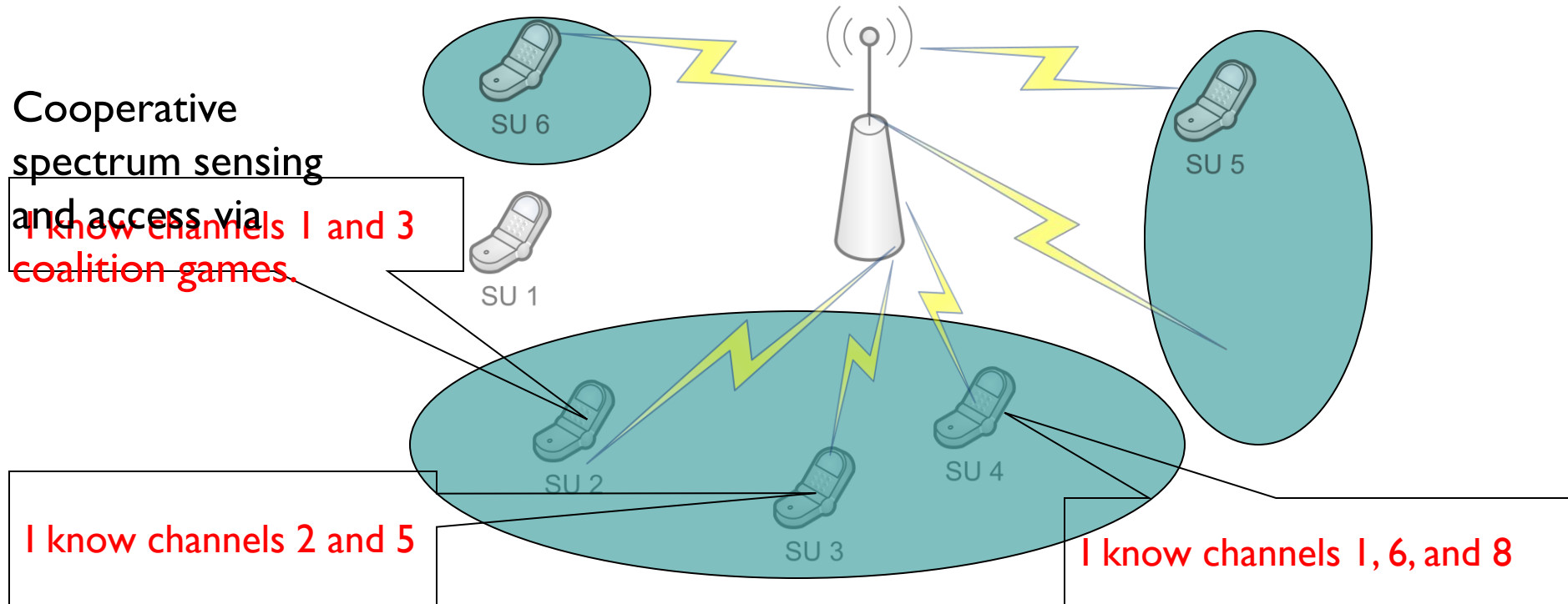
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- Can **SUs cooperate** to **reduce sensing time**, and use/learn **better channels**?

Cooperative Sensing and Access



Let's **cooperate** to enable:

- Spectrum **sensing/exploration gains** by sharing the statistics for the union of known channels
- Spectrum access (**capacity**) **gains** by **reducing interference**

Coalitional Games Preliminaries

- Coalitional game (N, v)
 - A set of players N , a **coalition** S is a group of cooperating players
 - Value (utility) of a coalition v and individual user payoff φ_i
 - **Goal:** analyze how coalitions form given benefits/costs for cooperation

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- **Characteristic form vs. Partition form**
 - When a coalition S forms or splits, does it affect the formation of the rest of the coalitions in the network?
 - **YES** => **Partition form**, **NO** => **Characteristic form**

Joint Sensing and Access as a Game

- SUs are the players whose goal is to reduce sensing time and boost their capacity by cooperating (e.g., by coordinating interference and learning new channels)
 - The individual utility will capture rate and sensing time when acting within the coalition S :

$$v_i(S, \Pi) = \bar{C}_i^S (1 - \tau_i^S)$$

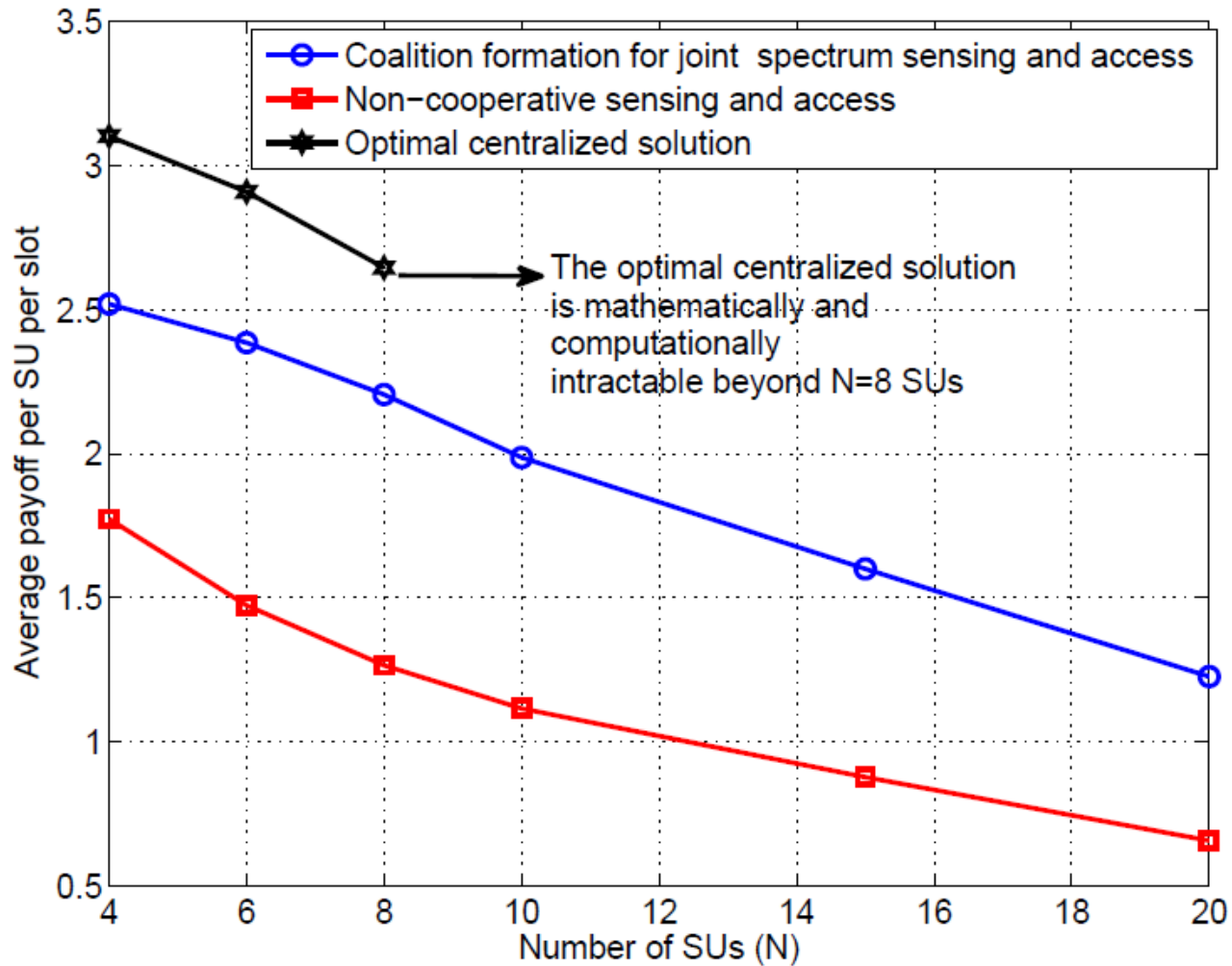
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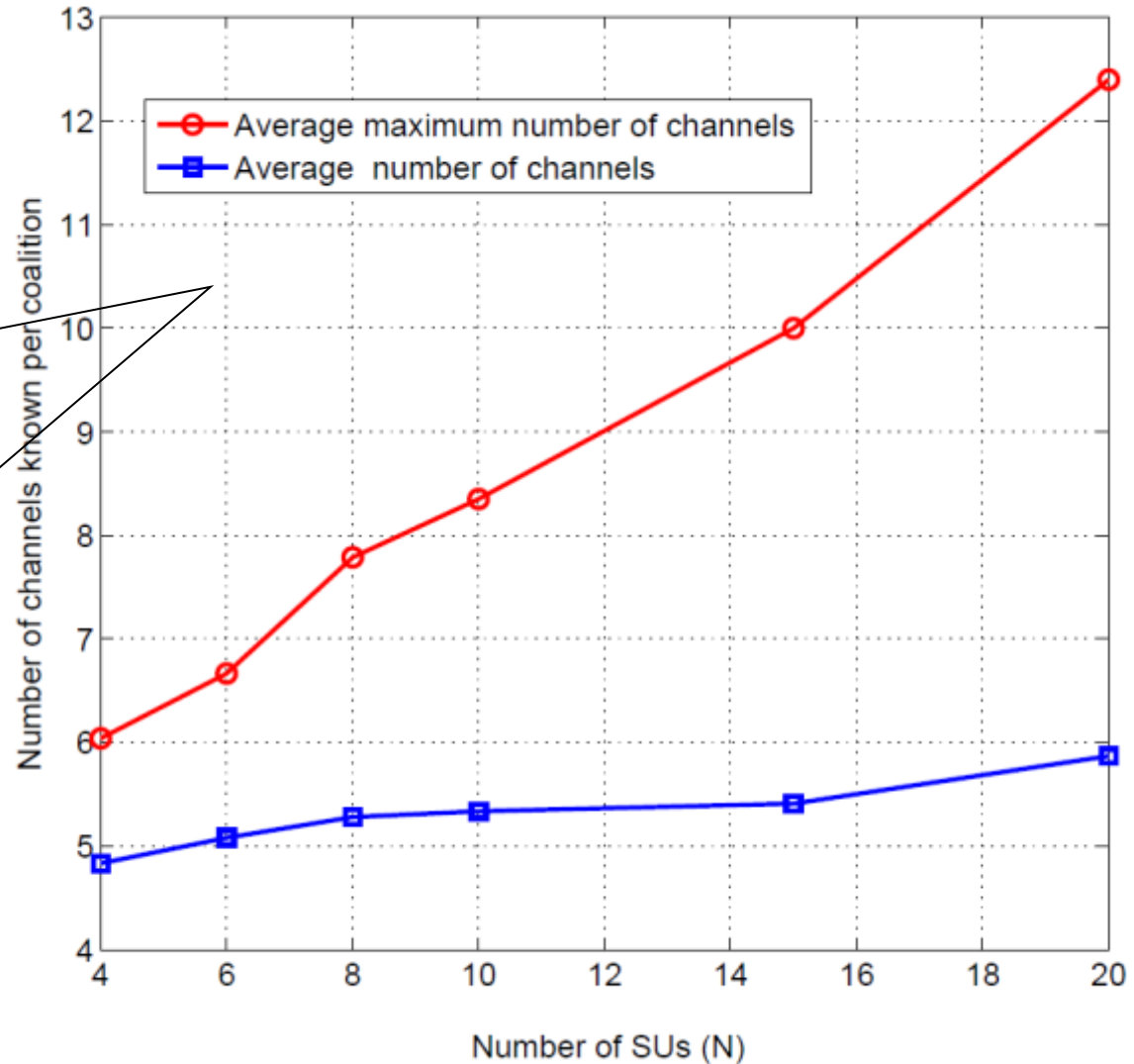
- **Key results and observations**
 - Utility depends on the entire partition => game has **partition form** and conventional coalition formation algorithms like merge/split do not work.
 - The game has NTU, since there is no transferable group utility.
 - An algorithm that is based on a “switch rule” whereby SUs change coalitions iteratively converges to a stable partition.
 - Stability in the Nash-sense: no SU has an incentive to leave current coalition

Simulation Results (I)



Simulation Results (2)

Using coalition formation, each group of SUs now has a clearer view of the overall spectrum.



Spectrum Monitoring

Motivation

- **How can SUs learn more** about the activity of the PU?

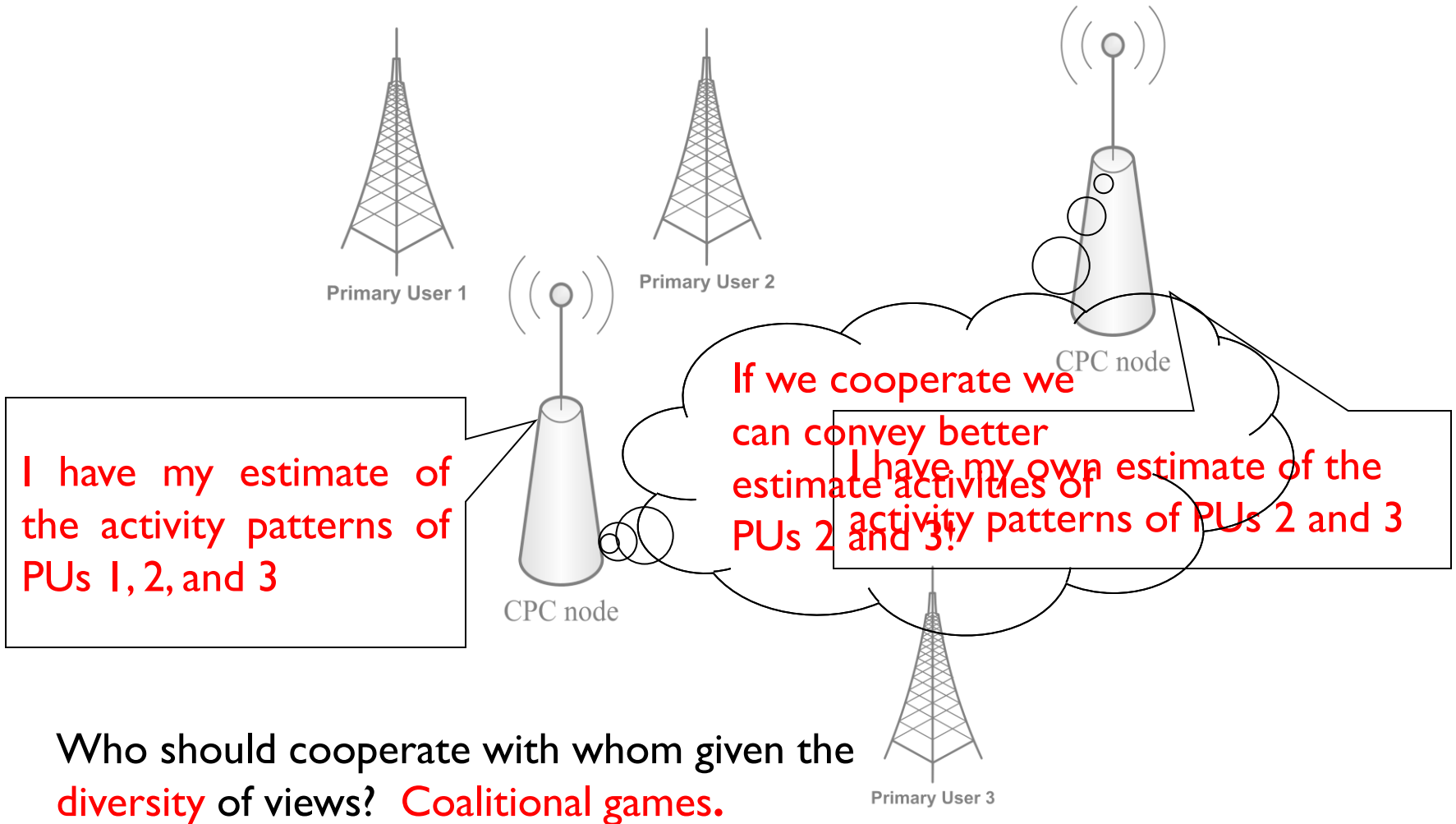
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- **Can the network help the SUs** understand the activity of the PU (e.g., its transmission pattern)?
- Use a **Cognitive Pilot Channel** (CPC) carried by either a dedicated device (CPC node) or by SUs themselves:
 - Introduced **for ensuring a conflict-free coexistence** of SUs and PUs
 - A **control channel** that can carry information in a given area **to assist cognitive users** in their **dynamic spectrum access**
 - Assist SUs in their operation by **identifying specific channels and operators for the SUs**, providing a better view on spectrum utilization, or providing advance spectrum management strategies

Problem Statement



Cooperative PU Monitoring as a Game

- When cooperating, the CPC nodes must **jointly** estimate the distribution of the PU activity pattern but...
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 - A coalition uses such techniques cooperatively to get an estimate of the PU activity (viewed as a pdf over the probability with which a PU is active)
- In our (NTU, characteristic form) game, CPC node i in coalition S optimizes

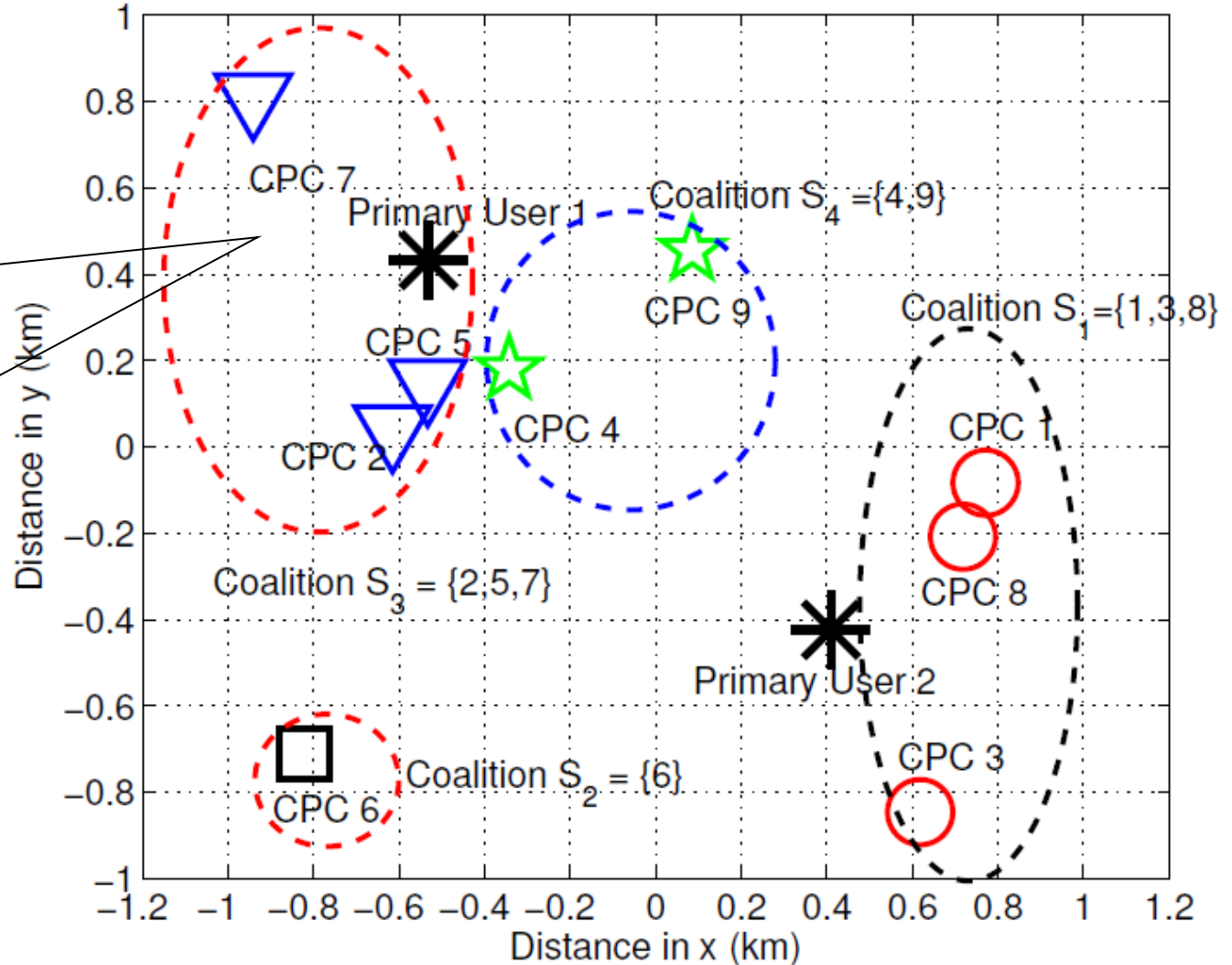
$$g_i(S) = \sum_{k \in \mathcal{K}} u_{ik}(S) - c(S)$$

Simple cost, linear with coalition size

Negative of the KL distance between two nonparametric estimates of channel k with different # observations

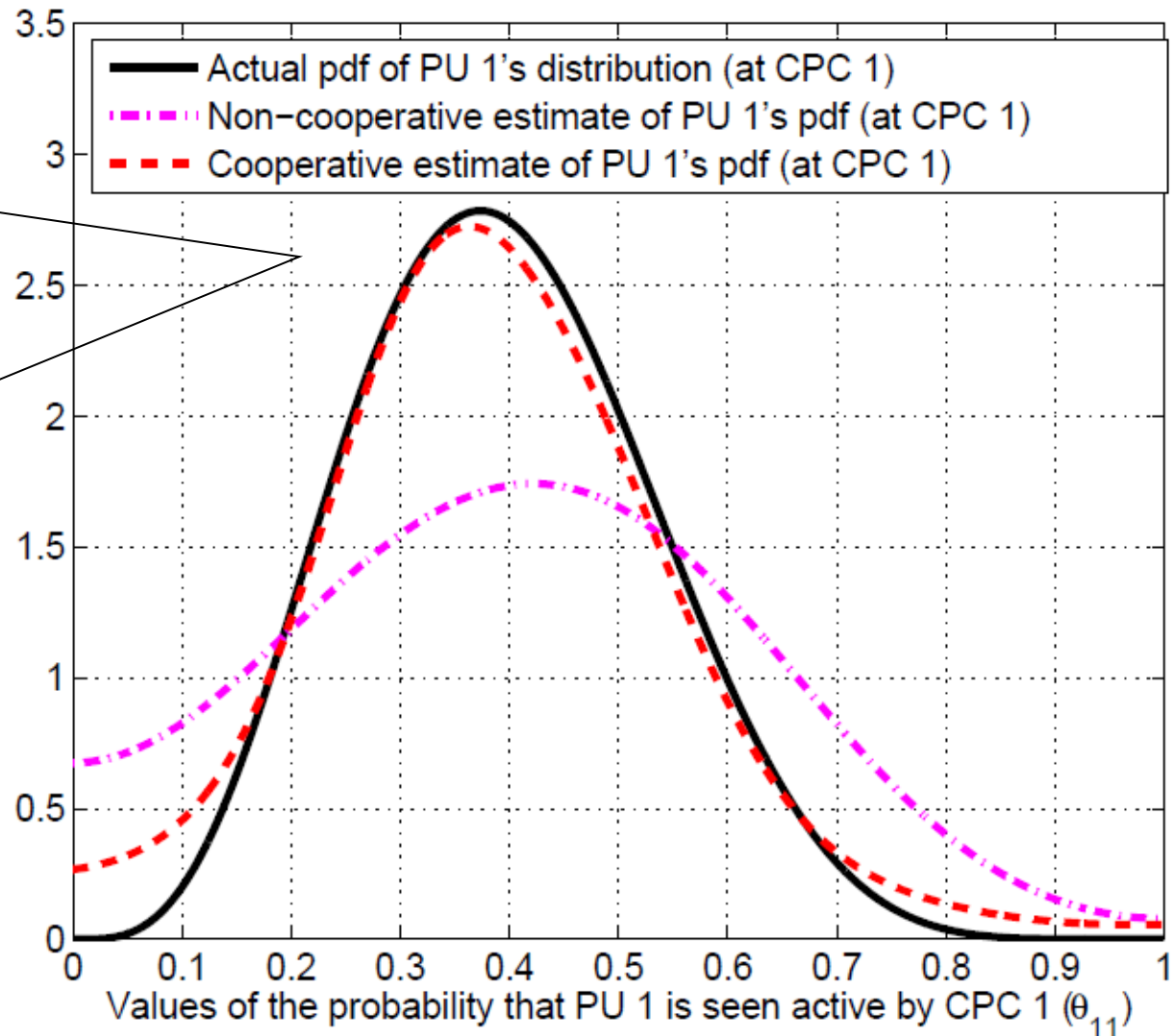
Simulation Results (I)

As per our intuition, CPC nodes that have overlapping PU views will cooperate.



Simulation Results (2)

Shows the accuracy of estimation using cooperation (this is CPC I from the previous slide).



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- Other areas of interest:
 - Cooperative communication among PUs (i.e., relaying)
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- Cognitive radio networks can benefit from cooperation among nodes.
- We've discussed two areas of cooperation:
 - Spectrum sensing and sharing
 - Spectrum monitoring by CPC nodes
- Other areas of interest:
 - Cooperative communication among PUs (i.e., relaying)
 - Cooperation between PUs and SUs
 - Experimentation on testbeds – CorteXlab!



Thank You!